

CompSci 516  
Database Systems

Lecture 7  
Design Theory and  
Normalization

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# What will we learn?

- What goes wrong if we have redundant info in a database?
- Why and how should you refine a schema?
- Functional Dependencies – a new kind of integrity constraints (IC)
- Normal Forms
- How to obtain those normal forms

# Example

The list of hourly employees in an organization

| <u>ssn (S)</u> | name (N)  | lot (L) | rating (R) | hourly-wage (W) | hours-worked (H) |
|----------------|-----------|---------|------------|-----------------|------------------|
| 111-11-1111    | Attishoo  | 48      | 8          | 10              | 40               |
| 222-22-2222    | Smiley    | 22      | 8          | 10              | 30               |
| 333-33-3333    | Smethurst | 35      | 5          | 7               | 30               |
| 444-44-4444    | Guldu     | 35      | 5          | 7               | 32               |
| 555-55-5555    | Madayan   | 35      | 8          | 10              | 40               |

- key = SSN

# Example

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| 555-55-5555    | Madayan   | 35      | 8          | 10              | 40               |

- key = SSN
- Suppose for a given rating, there is only one hourly\_wage value
- Redundancy in the table
- Why is redundancy bad?

# Why is redundancy bad? 1/4

The list of hourly employees in an organization

| <u>ssn (S)</u> | name (N)  | lot (L) | rating (R) | hourly-wage (W) | hours-worked (H) |
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| 555-55-5555    | Madayan   | 35      | 8          | 10              | 40               |

## 1. Redundant storage:

- Some information is stored repeatedly
- The rating value 8 corresponds to hourly\_wage 10, which is stored three times

# Why is redundancy bad? 2/4

The list of hourly employees in an organization

| <u>ssn (S)</u> | name (N)  | lot (L) | rating (R) | hourly-wage (W) | hours-worked (H) |
|----------------|-----------|---------|------------|-----------------|------------------|
| 111-11-1111    | Attishoo  | 48      | 8          | 10 → 9          | 40               |
| 222-22-2222    | Smiley    | 22      | 8          | 10              | 30               |
| 333-33-3333    | Smethurst | 35      | 5          | 7               | 30               |
| 444-44-4444    | Guldu     | 35      | 5          | 7               | 32               |
| 555-55-5555    | Madayan   | 35      | 8          | 10              | 40               |

## 2. Update anomalies

- If one copy of data is updated, an inconsistency is created unless all copies are similarly updated
- Suppose you update the hourly\_wage value in the first tuple using UPDATE statement in SQL -- inconsistency

# Why is redundancy bad? 3/4

The list of hourly employees in an organization

| <u>ssn (S)</u> | name (N)  | lot (L) | rating (R) | hourly-wage (W) | hours-worked (H) |
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| 444-44-4444    | Guldu     | 35      | 5          | 7               | 32               |
| 555-55-5555    | Madayan   | 35      | 8          | 10              | 40               |

### 3. Insertion anomalies:

- It may not be possible to store certain information unless some other, unrelated info is stored as well
- We cannot insert a tuple for an employee unless we know the hourly wage for the employee's rating value

# Why is redundancy bad? 4/4

The list of hourly employees in an organization

| <u>ssn (S)</u> | name (N)  | lot (L) | rating (R) | hourly-wage (W) | hours-worked (H) |
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| 555-55-5555    | Madayan   | 35      | 8          | 10              | 40               |

## 4. Deletion anomalies:

- It may not be possible to delete certain information without losing some other information as well
- If we delete all tuples with a given rating value (Attishoo, Smiley, Madayan), we lose the association between that rating value and its hourly\_wage value



# Nulls may or may not help

| <u>ssn (S)</u> | name (N)  | lot (L) | rating (R) | hourly-wage (W) | hours-worked (H) |
|----------------|-----------|---------|------------|-----------------|------------------|
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- Does not help redundant storage or update anomalies
- May help insertion and deletion anomalies
  - can insert a tuple with null value in the hourly\_wage field
  - but cannot record hourly\_wage for a rating unless there is such an employee (SSN cannot be null) – same for deletion

# Summary: Redundancy

Therefore,

- Redundancy arises when the schema forces an association between attributes that is “not natural”
- We want schemas that do not permit redundancy
  - at least identify schemas that allow redundancy to make an informed decision (e.g. for performance reasons)
- **Solution?**
  - **decomposition of schema**

# Decomposition

| <u>ssn (S)</u> | name (N)  | lot (L) | rating (R) | hourly-wage (W) | hours-worked (H) |
|----------------|-----------|---------|------------|-----------------|------------------|
| 111-11-1111    | Attishoo  | 48      | 8          | 10              | 40               |
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| <u>rating</u> | hourly_wage |
|---------------|-------------|
| 8             | 10          |
| 5             | 7           |

# More Decomposition

(on twitter)

| <i>uid</i> | <i>uname</i> | <i>twitterid</i> | <i>gid</i> | <i>fromDate</i> |
|------------|--------------|------------------|------------|-----------------|
| 142        | Bart         | @BartJSimpson    | dps        | 1987-04-19      |
| 123        | Milhouse     | @MilhouseVan_    | gov        | 1989-12-17      |
| 857        | Lisa         | @lisasimpson     | abc        | 1987-04-19      |
| 857        | Lisa         | @lisasimpson     | gov        | 1988-09-01      |
| 456        | Ralph        | @ralphwiggum     | abc        | 1991-04-25      |
| 456        | Ralph        | @ralphwiggum     | gov        | 1992-09-01      |
| ...        | ...          | ...              | ...        | ...             |

- User id
- user name
- Twitter id
- Group id
- Joining Date (to a group)

| <i>uid</i> | <i>uname</i> | <i>twitterid</i> |
|------------|--------------|------------------|
| 142        | Bart         | @BartJSimpson    |
| 123        | Milhouse     | @MilhouseVan_    |
| 857        | Lisa         | @lisasimpson     |
| 456        | Ralph        | @ralphwiggum     |
| ...        | ...          | ...              |

| <i>uid</i> | <i>gid</i> | <i>fromDate</i> |
|------------|------------|-----------------|
| 142        | dps        | 1987-04-19      |
| 123        | gov        | 1989-12-17      |
| 857        | abc        | 1987-04-19      |
| 857        | gov        | 1988-09-01      |
| 456        | abc        | 1991-04-25      |
| 456        | gov        | 1992-09-01      |
| ...        | ...        | ...             |

- Eliminates redundancy
- To get back to the original relation: ✕

# Unnecessary decomposition

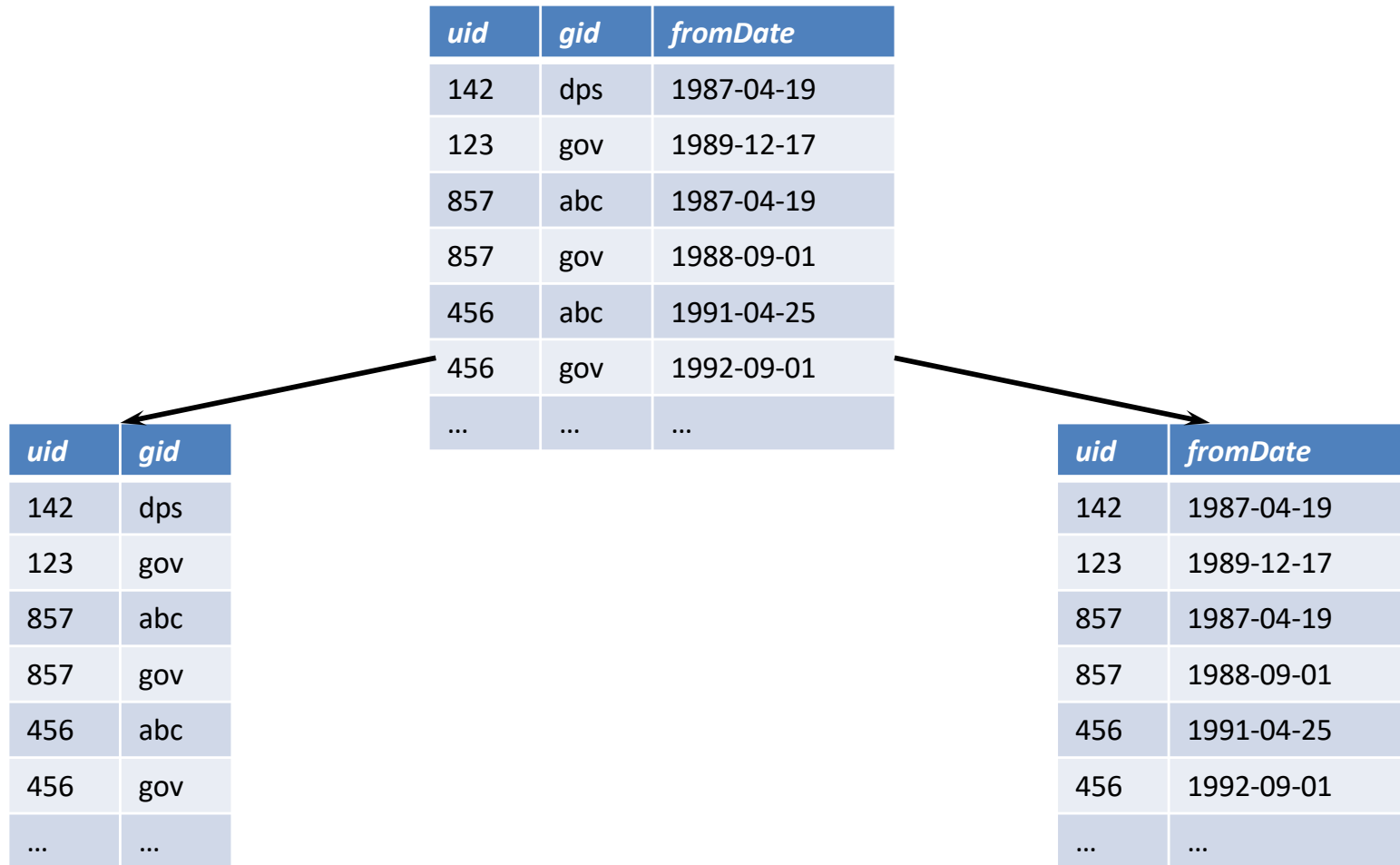
| <i>uid</i> | <i>uname</i> | <i>twitterid</i> |
|------------|--------------|------------------|
| 142        | Bart         | @BartJSimpson    |
| 123        | Milhouse     | @MilhouseVan_    |
| 857        | Lisa         | @lisasimpson     |
| 456        | Ralph        | @ralphwiggum     |
| ...        | ...          | ...              |

| <i>uid</i> | <i>uname</i> |
|------------|--------------|
| 142        | Bart         |
| 123        | Milhouse     |
| 857        | Lisa         |
| 456        | Ralph        |
| ...        | ...          |

| <i>uid</i> | <i>twitterid</i> |
|------------|------------------|
| 142        | @BartJSimpson    |
| 123        | @MilhouseVan_    |
| 857        | @lisasimpson     |
| 456        | @ralphwiggum     |
| ...        | ...              |

- Fine: join returns the original relation
- Unnecessary: no redundancy is removed; schema is more complicated (and *uid* is stored twice!)

# Bad decomposition



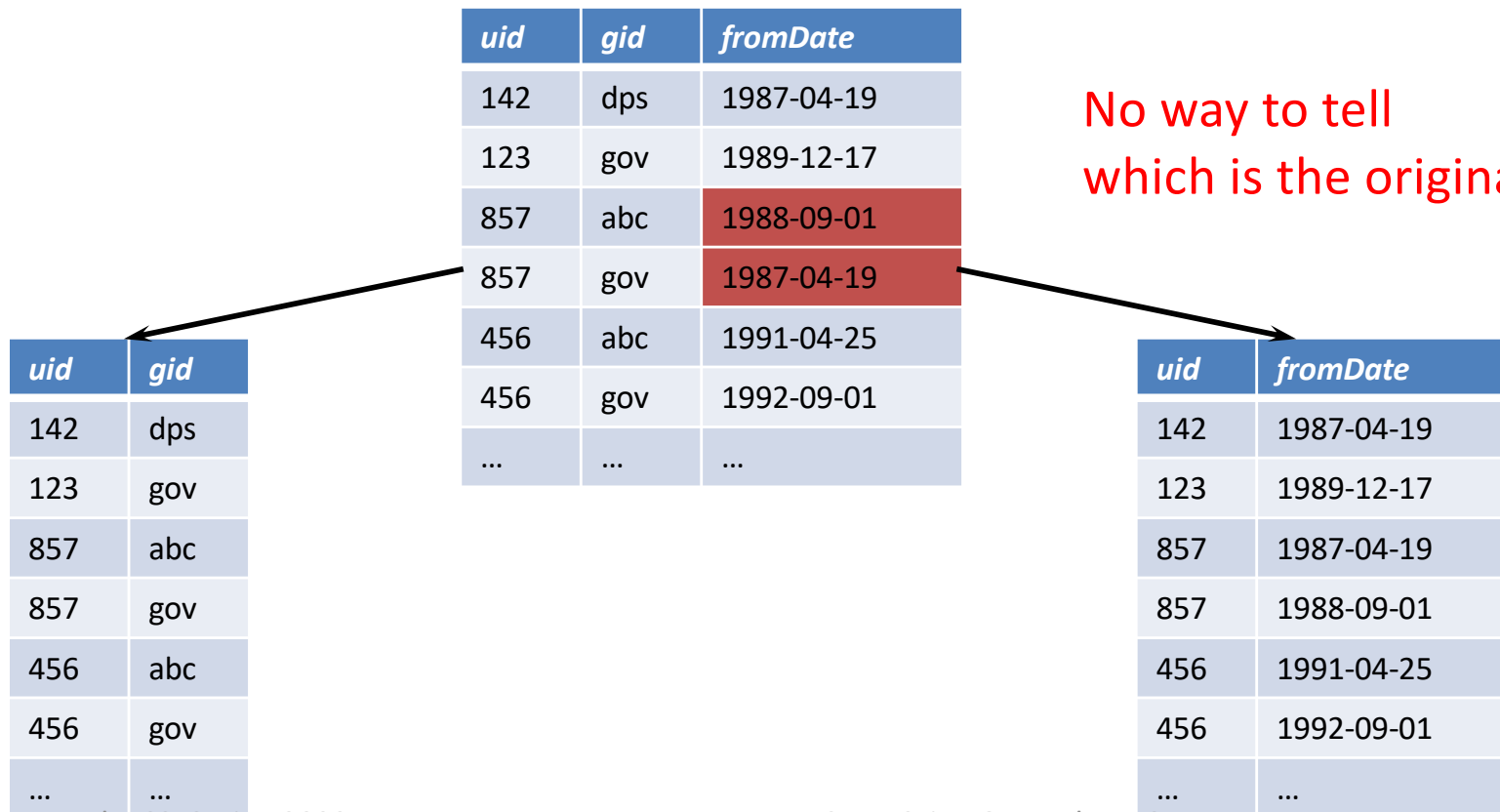
- Association between *gid* and *fromDate* is lost
- Join returns more rows than the original relation

# Lossless join decomposition

- Decompose relation  $R$  into relations  $S$  and  $T$ 
  - $attrs(R) = attrs(S) \cup attrs(T)$
  - $S = \pi_{attrs(S)}(R)$
  - $T = \pi_{attrs(T)}(R)$
- The decomposition is a **lossless join decomposition** if, given known constraints such as FD's, we can guarantee that  $R = S \bowtie T$
- $R \subseteq S \bowtie T$  or  $R \supseteq S \bowtie T$  ?
- Any decomposition gives  $R \subseteq S \bowtie T$  (why?)
  - A **lossy** decomposition is one with  $R \subset S \bowtie T$

# Loss? But I got more rows!

- “Loss” refers not to the loss of tuples, but to the loss of information
  - Or, the ability to distinguish different original relations





# Functional Dependencies (FDs)

- A functional dependency (FD)  $X \rightarrow Y$  holds over relation R if, for every allowable instance  $r$  of R:
  - i.e., given two tuples in  $r$ , if the X values agree, then the Y values must also agree
  - X and Y are *sets* of attributes
  - $t1 \in r, t2 \in r, \Pi_X(t1) = \Pi_X(t2)$  implies  $\Pi_Y(t1) = \Pi_Y(t2)$

| A  | B  | C  | D  |
|----|----|----|----|
| a1 | b1 | c1 | d1 |
| a1 | b1 | c1 | d2 |
| a1 | b2 | c2 | d1 |
| a2 | b1 | c3 | d1 |

What is a (possible) FD here?

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| a1 | b1 | c1 | d1 |
| a1 | b1 | c1 | d2 |
| a1 | b2 | c2 | d1 |
| a2 | b1 | c3 | d1 |

What is a (possible) FD here?

$AB \rightarrow C$

Note that, AB is not a key

not a correct question though.. see next slide!

# Functional Dependencies (FDs)

- An FD is a statement about **all** allowable relations
  - Must be identified based on semantics of application
  - Given some allowable instance  $r1$  of  $R$ , we can check if it **violates** some FD  $f$ , but we **cannot tell if  $f$  holds over  $R$**
- $K$  is a candidate key for  $R$  means that  $K \rightarrow R$ 
  - denoting  $R =$  all attributes of  $R$  too
  - However,  $S \rightarrow R$  does not require  $S$  to be minimal
  - e.g.,  $S$  can be a superkey

# Example

- Consider relation obtained from Hourly\_Emps:
  - Hourly\_Emps (ssn, name, lot, rating, hourly\_wage, hours\_worked)
- Use first letter of attributes for simplicity: **SNLRWH**
  - Basically the **set** of attributes {S,N,L,R,W,H}
- FDs on Hourly\_Emps:
  - **ssn is the key:**  $S \rightarrow \text{SNLRWH}$
  - **rating determines hourly\_wages:**  $R \rightarrow W$

# Armstrong's Axioms

- $X, Y, Z$  are sets of attributes
- **Reflexivity:** If  $X \supseteq Y$ , then  $X \rightarrow Y$
- **Augmentation:** If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$  for any  $Z$
- **Transitivity:** If  $X \rightarrow Y$  and  $Y \rightarrow Z$ , then  $X \rightarrow Z$

| A  | B  | C  | D  |
|----|----|----|----|
| a1 | b1 | c1 | d1 |
| a1 | b1 | c1 | d2 |
| a1 | b2 | c2 | d1 |
| a2 | b1 | c3 | d1 |

Apply these rules on  
 $AB \rightarrow C$  and check

# Additional Rules

- Follow from Armstrong's Axioms
- **Union:** If  $X \rightarrow Y$  and  $X \rightarrow Z$ , then  $X \rightarrow YZ$
- **Decomposition:** If  $X \rightarrow YZ$ , then  $X \rightarrow Y$  and  $X \rightarrow Z$

| A  | B  | C  | D  |
|----|----|----|----|
| a1 | b1 | c1 | d1 |
| a1 | b1 | c1 | d2 |
| a2 | b2 | c2 | d1 |
| a2 | b2 | c2 | d2 |

$A \rightarrow B, A \rightarrow C$

$A \rightarrow BC$

$A \rightarrow BC$

$A \rightarrow B, A \rightarrow C$

# Computing Attribute Closure

Algorithm:

- $\text{closure} = X$
- Repeat until no change
  - if there is an FD  $U \rightarrow V$  in  $F$  such that  $U \subseteq \text{closure}$ , then  $\text{closure} = \text{closure} \cup V$
- Does  $F = \{A \rightarrow B, B \rightarrow C, C D \rightarrow E\}$  imply  $A \rightarrow E$ ?
  - i.e, is  $A \rightarrow E$  in the closure  $F^+$ ? Equivalently, is  $E$  in  $A^+$ ?

# Computing FD Closure

- An FD  $f$  is **implied by** a set of FDs  $F$  if  $f$  holds whenever all FDs in  $F$  hold.
- $F^+$   
= **closure of  $F$**  is the set of all FDs that are implied by  $F$
- To check if a given FD  $X \rightarrow Y$  is in the closure of a set of FDs  $F$ 
  - No need to compute  $F^+$
  - Compute **attribute closure** of  $X$  (denoted  $X^+$ ) wrt  $F$ :
  - Check if  $Y$  is in  $X^+$

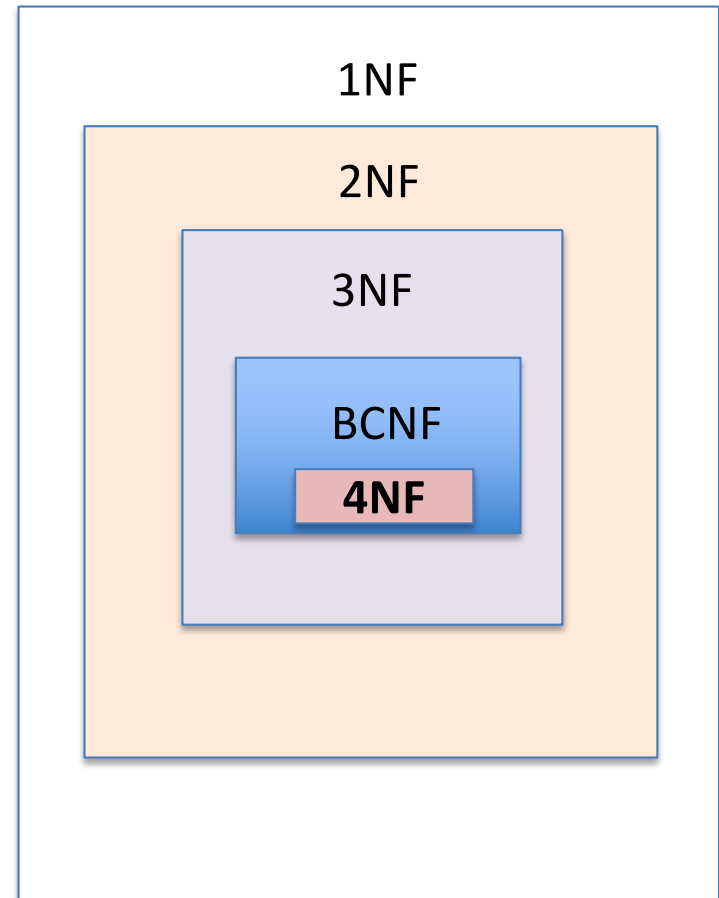


# Normal Forms

- What are the problems with decomposition?
  - Lossless joins (soon)
  - Performance issues -- decomposition may both
    - **help performance** (for updates, some queries accessing part of data), or
    - **hurt performance** (new joins may be needed for some queries)
- Given a schema, how to decide whether any schema refinement is needed at all?
  - If a relation is in a certain **normal forms**, it is known that certain kinds of problems are avoided/minimized
  - Helps us decide whether decomposing the relation is something we want to do

# Normal Forms

- R is in **4NF**
- ⇒ R is in **BCNF**
- ⇒ R is in 3NF
- ⇒ R is in 2NF (a historical one)
- ⇒ R is in 1NF (every field has atomic values)



Only BCNF and 4NF are covered in the class

# Boyce-Codd Normal Form (BCNF)

- Relation  $R$  with FDs  $F$  is in **BCNF** if, for all  $X \rightarrow A$  in  $F$ 
  - $A \in X$  (called a **trivial** FD), or
  - $X$  contains a key for  $R$ 
    - i.e.,  $X$  is a superkey

Intuitive idea:

$A \rightarrow B$ : Several tuples could have the same  $A$  value, and if so, they'll all have the same  $B$  value – redundancy – decomposition may be needed if  $A$  is not a key

if there is any non-key dependency, e.g.  $A \rightarrow B$ , decompose!

# BCNF decomposition algorithm

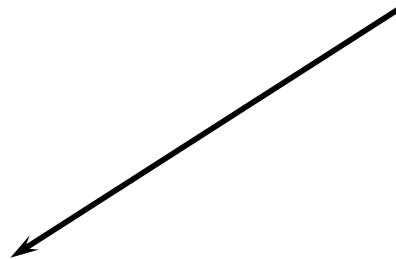
- Find a **BCNF violation**
  - That is, a non-trivial FD  $X \rightarrow Y$  in  $R$  where  $X$  is **not** a super key of  $R$
- Decompose  $R$  into  $R_1$  and  $R_2$ , where
  - $R_1$  has attributes  $X \cup Y$
  - $R_2$  has attributes  $X \cup Z$ , where  $Z$  contains all attributes of  $R$  that are in neither  $X$  nor  $Y$
- Repeat until all relations are in BCNF
- Also gives a lossless decomposition!

# BCNF decomposition example - 1

*uid* → *uname, twitterid*  
*twitterid* → *uid*  
*uid, gid* → *fromDate*

*UserJoinsGroup* (*uid, uname, twitterid, gid, fromDate*)

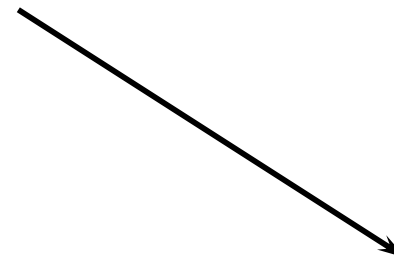
BCNF violation: *uid* → *uname, twitterid*



*User* (*uid, uname, twitterid*)

*uid* → *uname, twitterid*  
*twitterid* → *uid*

BCNF



*Member* (*uid, gid, fromDate*)

*uid, gid* → *fromDate*

BCNF

# BCNF decomposition example - 2

$uid \rightarrow uname, twitterid$   
 $twitterid \rightarrow uid$   
 $uid, gid \rightarrow fromDate$

*UserJoinsGroup* (*uid, uname, twitterid, gid, fromDate*)

BCNF violation:  $twitterid \rightarrow uid$

*UserId* (*twitterid, uid*)

BCNF

*UserJoinsGroup'* (*twitterid, uname, gid, fromDate*)

$twitterid \rightarrow uname$   
 $twitterid, gid \rightarrow fromDate$

BCNF violation:  $twitterid \rightarrow uname$

*UserName* (*twitterid, uname*)

BCNF

*Member* (*twitterid, gid, fromDate*)

BCNF

apply Armstrong's  
axioms and rules!

# BCNF decomposition example - 3

- CSJDPQV, key C,  $F = \{JP \rightarrow C, SD \rightarrow P, J \rightarrow S\}$ 
  - To deal with  $SD \rightarrow P$ , decompose into SDP, CSJDQV.
  - To deal with  $J \rightarrow S$ , decompose CSJDQV into JS and CJDQV
- Is  $JP \rightarrow C$  a violation of BCNF?
  - No
- Note:
  - several dependencies may cause violation of BCNF
  - The order in which we pick them may lead to very different sets of relations
  - there may be multiple correct decompositions (can pick  $J \rightarrow S$  first)

# BCNF = no redundancy?

- *User (uid, gid, place)*

- A user can belong to multiple groups
- A user can register places she's visited
- Groups and places have nothing to do with other

- FD's?

- None

- BCNF?

- Yes

- Redundancies?

- Tons!

| <i>uid</i> | <i>gid</i> | <i>place</i> |
|------------|------------|--------------|
| 142        | dps        | Springfield  |
| 142        | dps        | Australia    |
| 456        | abc        | Springfield  |
| 456        | abc        | Morocco      |
| 456        | gov        | Springfield  |
| 456        | gov        | Morocco      |
| ...        | ...        | ...          |



# Multivalued dependencies

- A multivalued dependency (MVD) has the form

$X \twoheadrightarrow Y$ , where  $X$  and  $Y$  are sets of attributes in a relation  $R$

- $X \twoheadrightarrow Y$  means that whenever two rows in  $R$  agree on all the attributes of  $X$ , then we can swap their  $Y$  components and get two rows that are also in  $R$

| $X$ | $Y$   | $Z$   |
|-----|-------|-------|
| $a$ | $b_1$ | $c_1$ |
| $a$ | $b_2$ | $c_2$ |
| $a$ | $b_2$ | $c_1$ |
| $a$ | $b_1$ | $c_2$ |
| ... | ...   | ...   |



# MVD examples

*User (uid, gid, place)*

- $uid \twoheadrightarrow gid$
- $uid \twoheadrightarrow place$ 
  - Intuition: given  $uid$ , attributes  $gid$  and  $place$  are “independent”
- $uid, gid \twoheadrightarrow place$ 
  - Trivial: LHS  $\cup$  RHS = all attributes of  $R$
- $uid, gid \twoheadrightarrow uid$ 
  - Trivial: LHS  $\supseteq$  RHS

# An elegant solution: “chase”

- Given a set of FD's and MVD's  $\mathcal{D}$ , does another dependency  $d$  (FD or MVD) follow from  $\mathcal{D}$ ?
- Procedure
  - Start with the premise of  $d$ , and treat them as “seed” tuples in a relation
  - Apply the given dependencies in  $\mathcal{D}$  repeatedly
    - If we apply an FD, we infer equality of two symbols
    - If we apply an MVD, we infer more tuples
  - If we infer the conclusion of  $d$ , we have a **proof**
  - Otherwise, if nothing more can be inferred, we have a **counterexample**

# Proof by chase

- In  $R(A, B, C, D)$ , does  $A \rightarrow B$  and  $B \rightarrow C$  imply that  $A \rightarrow C$ ?

Have:

| A | B              | C              | D              |
|---|----------------|----------------|----------------|
| a | b <sub>1</sub> | c <sub>1</sub> | d <sub>1</sub> |
| a | b <sub>2</sub> | c <sub>2</sub> | d <sub>2</sub> |

$A \rightarrow B$

|   |                |                |                |
|---|----------------|----------------|----------------|
| a | b <sub>2</sub> | c <sub>1</sub> | d <sub>1</sub> |
| a | b <sub>1</sub> | c <sub>2</sub> | d <sub>2</sub> |

$B \rightarrow C$

|   |                |                |                |
|---|----------------|----------------|----------------|
| a | b <sub>2</sub> | c <sub>1</sub> | d <sub>2</sub> |
| a | b <sub>2</sub> | c <sub>2</sub> | d <sub>1</sub> |

$B \rightarrow C$

|   |                |                |                |
|---|----------------|----------------|----------------|
| a | b <sub>1</sub> | c <sub>2</sub> | d <sub>1</sub> |
| a | b <sub>1</sub> | c <sub>1</sub> | d <sub>2</sub> |

Need:

| A | B              | C              | D              |
|---|----------------|----------------|----------------|
| a | b <sub>1</sub> | c <sub>2</sub> | d <sub>1</sub> |
| a | b <sub>2</sub> | c <sub>1</sub> | d <sub>2</sub> |



# Another proof by chase

- In  $R(A, B, C, D)$ , does  $A \rightarrow B$  and  $B \rightarrow C$  imply that  $A \rightarrow C$ ?

Have:

| <i>A</i> | <i>B</i>              | <i>C</i>              | <i>D</i>              |
|----------|-----------------------|-----------------------|-----------------------|
| <i>a</i> | <i>b</i> <sub>1</sub> | <i>c</i> <sub>1</sub> | <i>d</i> <sub>1</sub> |
| <i>a</i> | <i>b</i> <sub>2</sub> | <i>c</i> <sub>2</sub> | <i>d</i> <sub>2</sub> |

Need:

$$c_1 = c_2 \text{ ✌}$$

$$A \rightarrow B \quad b_1 = b_2$$

$$B \rightarrow C \quad c_1 = c_2$$

In general, with both MVD's and FD's, chase can generate both new tuples and new equalities

# Counterexample by chase

- In  $R(A, B, C, D)$ , does  $A \twoheadrightarrow BC$  and  $CD \rightarrow B$  imply that  $A \rightarrow B$ ?

Have:

| <i>A</i> | <i>B</i>              | <i>C</i>              | <i>D</i>              |
|----------|-----------------------|-----------------------|-----------------------|
| <i>a</i> | <i>b</i> <sub>1</sub> | <i>c</i> <sub>1</sub> | <i>d</i> <sub>1</sub> |
| <i>a</i> | <i>b</i> <sub>2</sub> | <i>c</i> <sub>2</sub> | <i>d</i> <sub>2</sub> |
| <i>a</i> | <i>b</i> <sub>2</sub> | <i>c</i> <sub>2</sub> | <i>d</i> <sub>1</sub> |
| <i>a</i> | <i>b</i> <sub>1</sub> | <i>c</i> <sub>1</sub> | <i>d</i> <sub>2</sub> |

$A \twoheadrightarrow BC$

Need:

$$b_1 = b_2 \text{ } \leftarrow$$

Counterexample!

# 4NF

- A relation  $R$  is in **Fourth Normal Form (4NF)** if
  - For every non-trivial MVD  $X \twoheadrightarrow Y$  in  $R$ ,  $X$  is a **superkey**
  - That is, all FD's and MVD's follow from “key  $\rightarrow$  other attributes” (i.e., no MVD's and no FD's besides key functional dependencies)
- **4NF is stronger than BCNF**
  - Because every FD is also a MVD

# 4NF decomposition algorithm

- Find a **4NF violation**
  - A non-trivial MVD  $X \twoheadrightarrow Y$  in  $R$  where  $X$  is **not** a superkey
- Decompose  $R$  into  $R_1$  and  $R_2$ , where
  - $R_1$  has attributes  $X \cup Y$
  - $R_2$  has attributes  $X \cup Z$  (where  $Z$  contains  $R$  attributes not in  $X$  or  $Y$ )
- Repeat until all relations are in 4NF
- Almost identical to BCNF decomposition algorithm
- Any decomposition on a 4NF violation is lossless



# 4NF decomposition example

| <i>uid</i> | <i>gid</i> | <i>place</i> |
|------------|------------|--------------|
| 142        | dps        | Springfield  |
| 142        | dps        | Australia    |
| 456        | abc        | Springfield  |
| 456        | abc        | Morocco      |
| 456        | gov        | Springfield  |
| 456        | gov        | Morocco      |
| ...        | ...        | ...          |

*User (uid, gid, place)*  
4NF violation: *uid*  $\twoheadrightarrow$  *gid*

*Member (uid, gid)*

4NF

| <i>uid</i> | <i>gid</i> |
|------------|------------|
| 142        | dps        |
| 456        | abc        |
| 456        | gov        |
| ...        | ...        |

*Visited (uid, place)*

4NF

| <i>uid</i> | <i>place</i> |
|------------|--------------|
| 142        | Springfield  |
| 142        | Australia    |
| 456        | Springfield  |
| 456        | Morocco      |
| ...        | ...          |

# Other kinds of dependencies and normal forms

- Dependency preserving decompositions
- Join dependencies
- Inclusion dependencies
- 5NF, 3NF, 2NF
- See book if interested (not covered in class)

# Summary



- Philosophy behind BCNF, 4NF:  
Data should depend on the key,  
the whole key,  
and nothing but the key!
  - You could have multiple keys though
- Redundancy is not desired typically
  - not always, mainly due to performance reasons
- Functional/multivalued dependencies – capture redundancy
- Decompositions – eliminate dependencies
- Normal forms
  - Guarantees certain non-redundancy
  - BCNF, and 4NF
- Lossless join
- How to decompose into BCNF, 4NF
- Chase